The flow of oil, in barrels per hour, through a pipeline on July 9 is given by the graph shown above. Of the following, which best approximates the total number of barrels of oil that passed through the pipeline that day?

a. 500  
b. 600  
c. 2,400  
d. 3,000  
e. 4,800

Insects destroyed a crop at the rate of \( \frac{100e^{-0.1t}}{2 - e^{-3t}} \) tons per day, where time \( t \) is measured in days. To the nearest ton, how many tons did the insects destroy during the time interval \( 7 \leq t \leq 14 \)?

a. 125  
b. 100  
c. 88  
d. 50  
e. 12

The rate of change of the altitude of a hot-air balloon is given by \( r(t) = t^3 - 4t^2 + 6 \) for \( 0 \leq t \leq 8 \). Which of the following expressions gives the change in altitude of the balloon during the time the altitude is decreasing?

a. \( \int_{1.572}^{3.514} r(t) \, dt \)  
b. \( \int_{0}^{6} r(t) \, dt \)  
c. \( \int_{0}^{2.667} r(t) \, dt \)  
d. \( \int_{1.572}^{3.514} r'(t) \, dt \)  
e. \( \int_{0}^{2.667} r'(t) \, dt \)
The graph of \( f' \), the derivative of \( f \), is the line shown in the figure above. If \( f(0) = 5 \), then \( f(1) = \)

a. 0  
b. 3  
c. 6  
d. 8  
e. 11

A particle moves along the x-axis so that at any time \( t > 0 \), its acceleration is given by \( a(t) = \ln(1 + 2^t) \). If the velocity of the particle is 2 at time \( t = 1 \), then the velocity of the particle at time \( t = 2 \) is

a. 0.462  
b. 1.690  
c. 2.555  
d. 2.886  
e. 3.346

A pizza, heated to a temperature of 350 degrees Fahrenheit (°F), is taken out of an oven and placed in a 75°F room at time \( t = 0 \) minutes. The temperature of the pizza is changing at a rate of \(-110e^{-0.4t}\) degrees Fahrenheit per minute. To the nearest degree, what is the temperature of the pizza at time \( t = 5 \) minutes?

a. 112°F  
b. 119°F  
c. 147°F  
d. 238°F  
e. 335°F
2. At an intersection in Thomasville, Oregon, cars turn left at the rate $L(t) = 60\sqrt{t} \sin^2 \left( \frac{t}{3} \right)$ cars per hour over the time interval $0 \leq t \leq 18$ hours. The graph of $y = L(t)$ is shown above.

(a) To the nearest whole number, find the total number of cars turning left at the intersection over the time interval $0 \leq t \leq 18$ hours.

(b) Traffic engineers will consider turn restrictions when $L(t) \geq 150$ cars per hour. Find all values of $t$ for which $L(t) \geq 150$ and compute the average value of $L$ over this time interval. Indicate units of measure.

(c) Traffic engineers will install a signal if there is any two-hour time interval during which the product of the total number of cars turning left and the total number of oncoming cars traveling straight through the intersection is greater than 200,000. In every two-hour time interval, 500 oncoming cars travel straight through the intersection. Does this intersection require a traffic signal? Explain the reasoning that leads to your conclusion.

2. The tide removes sand from Sandy Point Beach at a rate modeled by the function $R$, given by

$$R(t) = 2 + 5\sin \left( \frac{4\pi t}{25} \right).$$

A pumping station adds sand to the beach at a rate modeled by the function $S$, given by

$$S(t) = \frac{15t}{1 + 3t}. \quad \text{for } 0 \leq t \leq 6.$$ 

Both $R(t)$ and $S(t)$ have units of cubic yards per hour and $t$ is measured in hours for $0 \leq t \leq 6$. At time $t = 0$, the beach contains 2500 cubic yards of sand.

(a) How much sand will the tide remove from the beach during this 6-hour period? Indicate units of measure.

(b) Write an expression for $Y(t)$, the total number of cubic yards of sand on the beach at time $t$.

(c) Find the rate at which the total amount of sand on the beach is changing at time $t = 4$.

(d) For $0 \leq t \leq 6$, at what time $t$ is the amount of sand on the beach a minimum? What is the minimum value? Justify your answers.
4. Water is pumped into an underground tank at a constant rate of 8 gallons per minute. Water leaks out of the tank at the rate of $\sqrt{t} + 1$ gallons per minute, for $0 \leq t \leq 120$ minutes. At time $t = 0$, the tank contains 30 gallons of water.

(a) How many gallons of water leak out of the tank from time $t = 0$ to $t = 3$ minutes?

(b) How many gallons of water are in the tank at time $t = 3$ minutes?

(c) Write an expression for $A(t)$, the total number of gallons of water in the tank at time $t$.

(d) At what time $t$, for $0 \leq t \leq 120$, is the amount of water in the tank a maximum? Justify your answer.
This graph represents the rate of oil, in barrels per hour, so you need to find area under the curve to get barrels/hr = barrels. You should see 4 rectangles and 2 \( \frac{1}{2} \) rect. Each rectangle has an area of \( 6 \cdot 100 = 600 \). Take 600 times 5 rect \( \Rightarrow 3,000 \).

\[ \int_{0}^{14} \frac{1000e^{-1.1t}}{2-2e^{-3t}} \ dt = 124.994 \ldots \]

For this problem, graph the rate \( R(t) \) and find where \( R(t) < 0 \) because this will be where balloons altitude is dec.

The area of \( f'(x) \) represents \( f(x) \) so \( \int_{0}^{1} f'(x) \ dx = f(1) - f(0) \).  \( f(1) = \int_{0}^{1} f'(x) \ dx \)

\( f(0) = 5 \) (given) \( \int_{0}^{1} f'(x) \ dx = \frac{1}{2} (1)(4) = 3 \)

\[ a(t) = \ln(1+2^t) \cdot \ln(2) = 2 \] Find \( v(2) \).

Integrate \( a(t) \) to get \( v(t) \).

\[ \int_{1}^{2} \ln(1+2^t) \ dt = v(2) - v(1) \]

\[ v(2) = v(1) + \int_{1}^{2} \ln(1+2^t) \ dt \] (use calc)

\[ = 2 + 1.3463 \ldots = 3.346 \]

\[ r(t) = -100e^{-1.4t} \] where \( r(t) \) = rate pizza temp changing.

\[ X(t) = \text{Temp of pizza (to nearest degree)} \quad X(0) = 350 \]

\[ \int_{0}^{5} r(t) \ dt = X(5) - X(0) \Rightarrow X(5) = X(0) + \int_{0}^{5} (-100e^{-1.4t}) \ dt \]

\[ X(5) \approx 112.217 = 350 + (-237.783) \]
At an intersection in Thomasville, Oregon, cars turn left at the rate $L(t) = 60\sqrt{t}\sin^2\left(\frac{t}{3}\right)$ cars per hour over the time interval $0 \leq t \leq 18$ hours. The graph of $y = L(t)$ is shown above.

(a) To the nearest whole number, find the total number of cars turning left at the intersection over the time interval $0 \leq t \leq 18$ hours.

(b) Traffic engineers will consider turn restrictions when $L(t) \geq 150$ cars per hour. Find all values of $t$ for which $L(t) \geq 150$ and compute the average value of $L$ over this time interval. Indicate units of measure.

(c) Traffic engineers will install a signal if there is any two-hour time interval during which the product of the total number of cars turning left and the total number of oncoming cars traveling straight through the intersection is greater than 200,000. In every two-hour time interval, 500 oncoming cars travel straight through the intersection. Does this intersection require a traffic signal? Explain the reasoning that leads to your conclusion.

\[
\int_0^{18} L(t) \, dt = 1658 \text{ cars}
\]

\[
L(t) = 150 \text{ when } t = 12.42831, 16.12166
\]

\[
\int_R^S L(t) \, dt = 199.426 \text{ cars per hour}
\]

\[
\int_{13}^{15} L(t) \, dt = 431.931 > 400
\]

OR

The number of cars turning left will be greater than 400 on a two-hour interval if $L(t) \geq 200$ on that interval.

Yes, a traffic signal is required.
Question 2

The tide removes sand from Sandy Point Beach at a rate modeled by the function $R$, given by

$$R(t) = 2 + 5\sin\left(\frac{4\pi t}{25}\right).$$

A pumping station adds sand to the beach at a rate modeled by the function $S$, given by

$$S(t) = \frac{15t}{1 + 3t}.$$  

Both $R(t)$ and $S(t)$ have units of cubic yards per hour and $t$ is measured in hours for $0 \leq t \leq 6$. At time $t = 0$, the beach contains 2500 cubic yards of sand.

(a) How much sand will the tide remove from the beach during this 6-hour period? Indicate units of measure.

(b) Write an expression for $Y(t)$, the total number of cubic yards of sand on the beach at time $t$.

(c) Find the rate at which the total amount of sand on the beach is changing at time $t = 4$.

(d) For $0 \leq t \leq 6$, at what time $t$ is the amount of sand on the beach a minimum? What is the minimum value? Justify your answers.

(a) $\int_0^6 R(t) \, dt = 31.815$ or $31.816$ yd$^3$

(b) $Y(t) = 2500 + \int_0^t (S(x) - R(x)) \, dx$

(c) $Y'(t) = S(t) - R(t)$

$Y'(4) = S(4) - R(4) = -1.908$ or $-1.909$ yd$^3$/hr

(d) $Y'(t) = 0$ when $S(t) - R(t) = 0$.

The only value in $[0, 6]$ to satisfy $S(t) = R(t)$ is $a = 5.117865$.

<table>
<thead>
<tr>
<th>$t$</th>
<th>$Y(t)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>2500</td>
</tr>
<tr>
<td>$a$</td>
<td>2492.3694</td>
</tr>
<tr>
<td>6</td>
<td>2493.2766</td>
</tr>
</tbody>
</table>

The amount of sand is a minimum when $t = 5.117$ or 5.118 hours. The minimum value is 2492.369 cubic yards.
Water is pumped into an underground tank at a constant rate of 8 gallons per minute. Water leaks out of the tank at the rate of \( \sqrt{t+1} \) gallons per minute, for \( 0 \leq t \leq 120 \) minutes. At time \( t = 0 \), the tank contains 30 gallons of water.

(a) How many gallons of water leak out of the tank from time \( t = 0 \) to \( t = 3 \) minutes?

(b) How many gallons of water are in the tank at time \( t = 3 \) minutes?

(c) Write an expression for \( A(t) \), the total number of gallons of water in the tank at time \( t \).

(d) At what time \( t \), for \( 0 \leq t \leq 120 \), is the amount of water in the tank a maximum? Justify your answer.

\[ A(t) = 30 + \int_0^t (8 - \sqrt{x + 1}) \, dx \]

\[ A(t) = 30 + 8t - \frac{2}{3} (t + 1)^{3/2} + C \]

\[ A'(t) = 8 - \sqrt{t+1} = 0 \text{ when } t = 63 \]

\[ A'(t) \text{ is positive for } 0 < t < 63 \text{ and negative for } 63 < t < 120. \]

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